

**2020** TEST 5

## **MATHEMATICS METHODS Year 11**

Section One: Calculator-free

Your name	Marking	Key	
		0	
Teacher's nar	me		

## Time and marks available for this section

Working time:

30 minutes

Marks available:

27 marks

# Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items:

nil

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

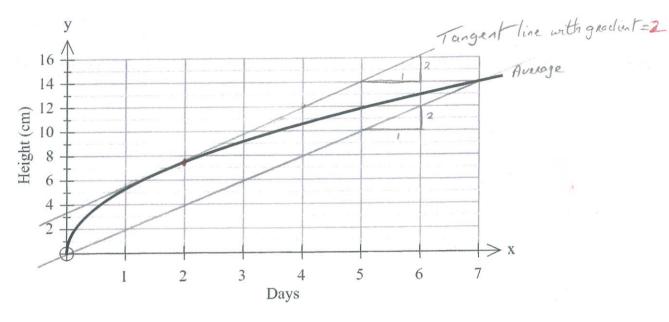
#### Instructions to candidates

- 1. The rules of conduct of the CCGS assessments are detailed in the Reporting and Assessment Policy. Sitting this assessment implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet using a blue/black pen. Do not use erasable or gel pens.
- 3. Answer all questions.
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- 6. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 7. It is recommended that **you do not use pencil**, except in diagrams.

(3 marks)

The graph below shows the growth of bean plants over the seven days following the first appearance of the sprout.

3



(a) Calculate the average rate of growth over the seven days.

(1 mark)

Calculates gradient from (0.0) to (7,14) connectly.

(b) On what day does the instantaneous growth rate appear to be equal to the seven-day average growth rate. Draw a tangent on the graph at this point.

= 2 cm/day V

Day 2

(2 marks)

Draws tangent with gradient of 2

Identifies day 2

(5 marks)

Determine the derivative of the following functions.

(a) 
$$f(x) = 7x^3 - 2x^2 - x - 6$$

(1 mark)

$$f'(x) = 21x^2 - 4x - 1$$

Connectly determines desirative

(b) 
$$f(x) = 2\pi x + \frac{x^3}{3} - \frac{x^4}{5}$$

(2 marks)

$$f(x) = 2TT + x^2 - \frac{1}{5}x^3$$

Correctly differentiates a term V Correctly differentiates x3 and I to

(c) 
$$f(x) = (2x-1)^2$$

(2 marks)

$$(2x-1)^{2} = (2x-1)(2x-1)$$
  
=  $4x^{2}-4x+1$  Expands  $f(x)$ 

$$f(x) = 8x - 4$$

V Differentiates connectly

(5 marks)

Consider the function  $v = t^3 - 5t^2$ 

(2 marks) Determine the instantaneous rate of change of the function at t = 2. (a)

5

$$y' = 3t^2 - 10t$$
  
 $y'(t=2) = 3(2)^2 - 10(2)$   
 $= -8$ 

I substitutes into decirative connectly V Evaluates connectly

When is the instantaneous rate of change of y equal to 25?

(3 marks)

$$3t^2 - 10t = 25$$

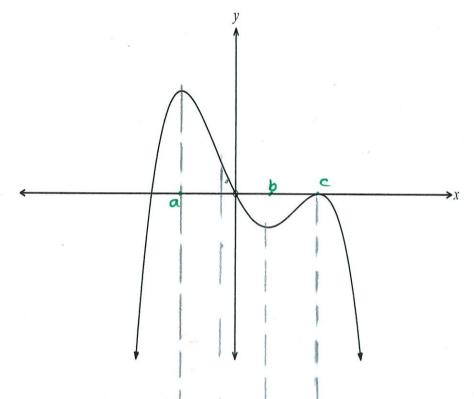
V Formulates correct equation

$$3t^2 - 10t - 25 = 0$$

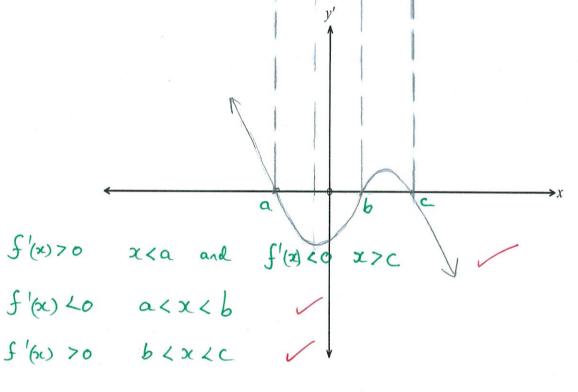
(3t+5)(t-5)=0 V Factorises correctly

(3 marks)

A function has been drawn on the axes below



Draw the gradient function for this function on the axes below.



Graph of gradient function must line up connectly with original function.

See next page

(4 marks)

The tangent to the curve  $y = 8x - 2 - 2x^2$  at the point (3,4) intersects the x-axis at (a,0). Determine the value of a.

41 = 8-400

States correct derivative

9 (x=3) = 8-12

= -4 gradient of tangent / calculates connect gradient

Equation of tangent: y = -4x+c

Using (3,4)

4 = -4(3) + (

16 = c / Calculates c correctly

Excuation of tangent: y = -4x+16

x intercept

: 0 = -401 + 16

oc = 4

V States correct value for a

(7 marks)

Consider the function  $f(x) = x^2 - 5x$ 

(a) Use first principles to differentiate the function f(x).

(3 marks)

$$f(x+h) = (x+h)^{2} - 5(x+h)$$

$$= x^{2} + 2xh + h^{2} - 5x - 5h$$

$$f(x+h) - f(x) = x^{2} + 2xh + h^{2} - 5x - 5h - x^{2} + 5x$$

$$= 2xh + h^{2} - 5h \quad \text{consectly evaluates}$$

$$f(x+h) - f(x) = \frac{2xh + h^{2} - 5h}{h}$$

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} \frac{2xh + h^{2} - 5h}{h}$$

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} \frac{2xh + h^{2} - 5h}{h}$$

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} \frac{(2x+h-5)}{h} \xrightarrow{\text{limit}}$$

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} (2x+h-5)$$

$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} (2x+h-5)$$

8

$$\lim_{h\to 0} \frac{f(x+h) - f(x)}{h} = 2x - 5$$

Factorises to remove h and evaluates connectly

$$\frac{df}{dx} = 2x - 5$$

if "lim" not included on R.H.S. -I mark.

### Question 6 continued

Determine the gradient of f(x) when x = 2(b)

(1 mark)

$$f'(2) = 2(2) -5$$
  
= -1

Evaluates f(2) correctly

Write the equation of the tangent to f(x) at x = 2(c)

(3 marks)

$$y = -1 \times + C$$

$$f(x) = x^{2} - 5 \times X$$

$$f(y) = -6$$

$$-6 = -1(2) + C$$

$$(2,-6)$$

$$-4 = C$$

$$Fquation with correct gradient (i.e. m = -1)$$

$$y = -1 \times -4$$

$$Calculates c correctly$$

$$Fquation:  $y = -x - 4$ 

$$States equation$$$$

Additional working space

Question number: \_\_\_\_\_

11

## CALCULATOR-FREE

Additional working space

Question number:



**2020** TEST 5

# **MATHEMATICS METHODS Year 11**

Section I wo:		
Calculator-assumed		
	A 1	

Your name	Marking	Key.	
	9	d	
Teacher's na	ime		

### Time and marks available for this section

Working time:

15 minutes

Marks available:

12 marks

## Materials required/recommended for this section

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Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

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Special items: dr

drawing instruments, templates and up to three calculators approved

for use in this assessment

Important note to candidates

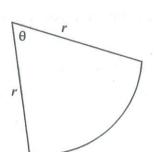
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(5 marks)

Part of a local children's playground, in the shape of a circular sector, is to have a new rubber surface installed.



Perimeter =  $2\pi R \times 2\pi + 2R$  20 = RO + 2Retc.

(a) If the perimeter of this sector is 20 metres, then show that  $\theta$  can be expressed as

$$\theta = \frac{20}{r} - 2 \tag{2 marks}$$

Perimeter = R+R+RO  
= 2R+RO  

$$2R+RO = 20$$
  
 $RO = 20-2R$   
 $O = 20-2R$   
 $O = 20-2R$ 

states correct equation for perimeter.

Re arranges to express in correct form.

(b) Hence, or otherwise, determine the angle and the radius required to maximise the area of the rubber surface.

(3 marks)

$$A = \frac{1}{2}R^{2}O$$

$$= \frac{R^{2}}{2}(\frac{20}{R}-2)$$

$$= 10R - R^{2}$$

$$\leq \frac{10R - R^{2}}{R}$$

Max 
$$\Rightarrow$$
  $10-2R=0$ 
 $R=5$ 
Differentiates and solves for  $R$ 
 $0 = \frac{20}{5}-2$ 
 $= 2 \text{ radians.}$ 
 $= 2 \text{ radians.}$ 
See next page

(7 marks)

Consider the quartic function  $y = 3x^4 - 4x^3 - 12x^2 + 12$ ,

State the coordinates of any stationary points and give the nature of each. (a)

(3 marks)

From calculator

V correct maximum

(0,12) maximum

Points must be identified.

(b) For what values of x is the function decreasing.

(2 marks).

if y cooks not given (3) marks

x <-1 and 0 < > < 2

Correct inequality for correct inequality

(c) Determine the global maximum and the global minimum values for this function in the interval  $-2 \le x \le 3$ . (2 marks)

Global maximum 44 at x=-2 V States correct global max

Global minimum -20 at x = 2 /states correct global min.

Additional working space

Question number: \_\_\_\_\_

Additiona	l working	space
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Question number: \_\_\_\_\_